

Scalar–Isovector δ -meson in RMF Theory and the Quark Deconfinement Phase Transition in Neutron Stars

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Introduction

RMF-theory:

$\sigma \omega \rho$

J.D.Walecka, Ann.Phys. 87, 4951, 1974

B.D.Serot, J.D.Walecka, Int.J.Mod.Phys. E6, 515, 1997.

Low density asymmetric nuclear matter:

$\sigma \omega \rho \delta$

S.Kubis, M.Kutschera, Phys. Lett., B399,191,1997.

B.Liu, V.Greco, V.Baran, M.Colonna, M.Di Toro, Phys. Rev. C65, 045201, 2002.

Heavy ion collisions at intermediate energies:

$\sigma \omega \rho \delta$

V.Greco, M.Colonna, M.Di Toro, F.Matera, Phys. Rev. C67, 015203, 2003

V.Greco et al., Phys. Lett. B562, 215, 2003.

T.Gaitanos, M.Colonna, M.Di Toro, H.H.Wolter, Phys.Lett. B595, 209,2004.

Neutron stars without quark deconfinement:

$\sigma \omega \rho \delta$

B.Liu, H.Guo, M.Di Toro, V.Greco, arXiv Nucl-th/0409014 v2, 2005

Lagrangian density of many-particle system of $p, n, \sigma, \omega, \rho, \delta$

$$\begin{aligned} \mathcal{L} = & \bar{\psi}_N \left[\gamma^\mu \left(i\partial_\mu - g_\omega \omega_\mu(x) - \frac{1}{2} g_\rho \vec{\tau}_N \cdot \vec{\rho}_\mu(x) \right) - \left(m_N - g_\sigma \sigma(x) - g_\delta \vec{\tau}_N \cdot \vec{\delta}(x) \right) \right] \psi_N + \\ & + \frac{1}{2} \left(\partial_\mu \sigma(x) \partial^\mu \sigma(x) - m_\sigma^2 \sigma(x)^2 \right) - U(\sigma(x)) + \frac{1}{2} m_\omega^2 \omega^\mu(x) \omega_\mu(x) - \frac{1}{4} \Omega_{\mu\nu}(x) \Omega^{\mu\nu}(x) + \\ & + \frac{1}{2} \left(\partial_\mu \vec{\delta}(x) \partial^\mu \vec{\delta}(x) - m_\delta^2 \vec{\delta}(x)^2 \right) + \frac{1}{2} m_\rho^2 \vec{\rho}^\mu(x) \vec{\rho}_\mu(x) - \frac{1}{4} R_{\mu\nu}(x) R^{\mu\nu}(x), \end{aligned}$$

$$x = x_\mu = (t, x, y, z) \quad \sigma(x), \omega_\mu(x), \vec{\delta}(x), \vec{\rho}_\mu(x) \quad \psi_N = \begin{pmatrix} \psi_p \\ \psi_n \end{pmatrix}$$

$$U(\sigma) = \frac{b}{3} m_N (g_\sigma \sigma)^3 + \frac{c}{4} (g_\sigma \sigma)^4,$$

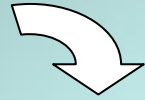
$$\Omega_{\mu\nu}(x) = \partial_\mu \omega_\nu(x) - \partial_\nu \omega_\mu(x),$$

$$\mathcal{R}_{\mu\nu}(x) = \partial_\mu \rho_\nu(x) - \partial_\nu \rho_\mu(x).$$

	Scalar	Vector
Isoscalar	σ	ω
Isovector	δ	ρ

Relativistic mean-field approach

$$\frac{\partial \mathcal{L}}{\partial \phi(x)} - \partial_\mu \frac{\partial \mathcal{L}}{\partial (\partial_\mu \phi(x))} = 0$$



$$e_p(k) = \sqrt{k^2 + m_p^{*2}} + g_\omega \bar{\omega}_0 + \frac{1}{2} g_\rho \bar{\rho}_0^{(3)},$$

$$e_n(k) = \sqrt{k^2 + m_n^{*2}} + g_\omega \bar{\omega}_0 - \frac{1}{2} g_\rho \bar{\rho}_0^{(3)},$$

$$m_\sigma^2 \bar{\sigma} = g_\sigma \left(n_{sp} + n_{sn} - \frac{dU(\bar{\sigma})}{d\bar{\sigma}} \right),$$

$$m_\omega^2 \bar{\omega} = g_\omega (n_p + n_n),$$

$$m_\delta^2 \bar{\delta}^{(3)} = g_\delta (n_{sp} - n_{sn}),$$

$$m_\rho^2 \bar{\rho}_0^{(3)} = \frac{1}{2} g_\rho (n_p - n_n),$$

$$m_p^* = m_N - g_\sigma \bar{\sigma} - g_\delta \bar{\delta}^{(3)},$$

$$m_n^* = m_N - g_\sigma \bar{\sigma} + g_\delta \bar{\delta}^{(3)}.$$

$$n_p = \frac{k_{Fp}^3}{3\pi^2}, \quad n_n = \frac{k_{Fn}^3}{3\pi^2},$$

$$n_{sp} = \frac{1}{\pi^2} \int_0^{k_{Fp}} \frac{m_p^*}{\sqrt{k^2 + m_p^{*2}}} k^2 dk,$$

$$n_{sn} = \frac{1}{\pi^2} \int_0^{k_{Fn}} \frac{m_n^*}{\sqrt{k^2 + m_n^{*2}}} k^2 dk.$$

$$\mu_p = e_p(k_{Fp}) = \sqrt{k_{Fp}^2 + m_p^{*2}} + g_\omega \bar{\omega}_0 + \frac{1}{2} g_\rho \bar{\rho}_0^{(3)},$$

$$\mu_n = e_n(k_{Fn}) = \sqrt{k_{Fn}^2 + m_n^{*2}} + g_\omega \bar{\omega}_0 - \frac{1}{2} g_\rho \bar{\rho}_0^{(3)}.$$

Parametric EOS for nuclear matter

$$g_\sigma \bar{\sigma} \equiv \sigma, \quad g_\omega \bar{\omega}_0 \equiv \omega, \quad g_\delta \bar{\delta}^{(3)} \equiv \delta, \quad g_\rho \bar{\rho}^{(3)} \equiv \rho,$$

$$\left(\frac{g_\sigma}{m_\sigma}\right)^2 \equiv a_\sigma, \quad \left(\frac{g_\omega}{m_\omega}\right)^2 \equiv a_\omega, \quad \left(\frac{g_\delta}{m_\delta}\right)^2 \equiv a_\delta, \quad \left(\frac{g_\rho}{m_\rho}\right)^2 \equiv a_\rho, \quad \alpha = \frac{n_n - n_p}{n}, \text{ the asymmetry parameter}$$

$$P(n, \alpha) = \frac{1}{\pi^2} \int_0^{k_F(n)(1-\alpha)^{1/3}} \left(\sqrt{k_F(n)^2(1-\alpha)^{2/3} + (m_N - \sigma - \delta)^2} - \sqrt{k^2 + (m_N - \sigma - \delta)^2} \right) k^2 dk +$$

$$+ \frac{1}{\pi^2} \int_0^{k_F(n)(1+\alpha)^{1/3}} \left(\sqrt{k_F(n)^2(1+\alpha)^{2/3} + (m_N - \sigma + \delta)^2} - \sqrt{k^2 + (m_N - \sigma + \delta)^2} \right) k^2 dk -$$

$$- \tilde{U}(\sigma) + \frac{1}{2} \left(-\frac{\sigma^2}{a_\sigma} + \frac{\omega^2}{a_\omega} - \frac{\delta^2}{a_\delta} + \frac{\rho^2}{a_\rho} \right).$$

$$\varepsilon(n, \alpha) = \frac{1}{\pi^2} \int_0^{k_F(n)(1-\alpha)^{1/3}} \sqrt{k^2 + (m_N - \sigma - \delta)^2} k^2 dk +$$

$$+ \frac{1}{\pi^2} \int_0^{k_F(n)(1+\alpha)^{1/3}} \sqrt{k^2 + (m_N - \sigma + \delta)^2} k^2 dk + \tilde{U}(\sigma) + \frac{1}{2} \left(\frac{\sigma^2}{a_\sigma} + \frac{\omega^2}{a_\omega} + \frac{\delta^2}{a_\delta} + \frac{\rho^2}{a_\rho} \right),$$

Parameters of RMF theory

$$a_\sigma, a_\omega, a_\delta, a_\rho, b, c$$

Symmetric nuclear matter ($\alpha = 0$)

Saturation density ($n = n_0$)

$$m_N^* = \gamma m_N, \quad \sigma_0 = (1 - \gamma) m_N$$

$$\left. \frac{d\varepsilon(n, \alpha)}{dn} \right|_{\substack{n=n_0 \\ \alpha=0}} = \frac{\varepsilon(n_0, 0)}{n_0} = m_N + f_0, \quad f_0 = \frac{B}{A}, \quad \text{Binding energy per baryon}$$

$$a_\omega = \frac{1}{n_0} \left(m_N + f_0 - \sqrt{k_F(n_0)^2 + (m_N - \sigma_0)^2} \right)$$

$$\omega_0 = a_\omega n_0 = m_N + f_0 - \sqrt{k_F(n_0)^2 + (m_N - \sigma_0)^2}$$

$$\frac{\sigma_0}{a_\sigma} = \frac{2}{\pi^2} \int_0^{k_F(n_0)} \frac{(m_N - \sigma_0)}{\sqrt{k^2 + (m_N - \sigma_0)^2}} k^2 dk - b m_N \sigma_0^2 - c \sigma_0^3$$

Parameters of RMF theory

$$\varepsilon_0 = n_0(m_N + f_0) = \frac{2}{\pi^2} \int_0^{k_F(n_0)} \sqrt{k^2 + (m_N - \sigma_0)^2} k^2 dk + \frac{b}{3} m_N \sigma_0^3 + \frac{c}{4} \sigma_0^4 + \frac{1}{2} \left(\frac{\sigma_0^2}{a_\sigma} + n_0^2 a_\omega \right)$$

$$K = 9 n_0^2 \left. \frac{d^2}{dn^2} \left(\frac{\varepsilon(n, \alpha)}{n} \right) \right|_{\substack{n=n_0 \\ \alpha=0}} \quad \text{compressibility module}$$

$$\frac{\varepsilon_{sym}}{n} = E_{sym}(n) \alpha^2 \quad \longrightarrow \quad E_{sym}(n) = \frac{1}{2n} \left. \frac{d^2 \varepsilon(n, \alpha)}{d\alpha^2} \right|_{\alpha=0}$$

Symmetry energy

$$m_N = 938,93 \text{ MeV}$$

$$n_0 = 0,153 \text{ fm}^{-3}$$

$$\gamma = \frac{m_N^*}{m_N} = 0,78$$

$$K = 300 \text{ MeV}$$

$$f_0 = -16,3 \text{ MeV}$$

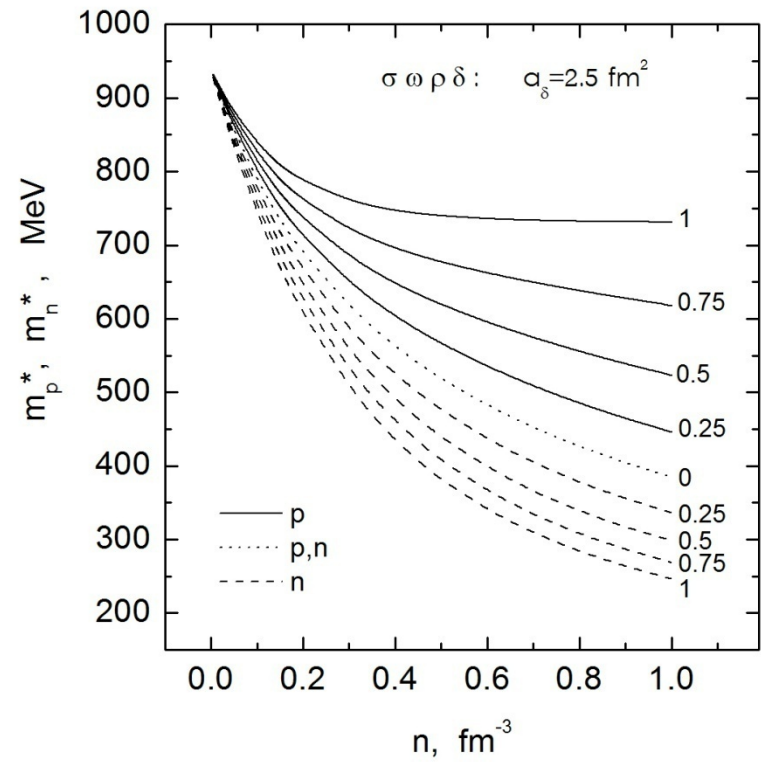
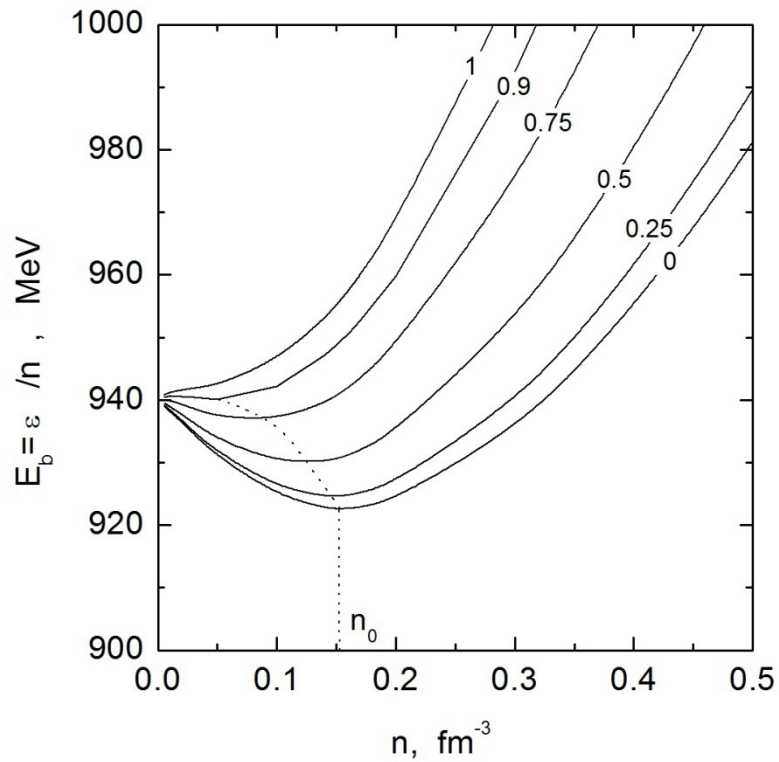
$$E_{sym}^{(0)} = 32,5 \text{ MeV}$$

$a_\delta \text{ fm}^2$	0	0,5	1	1,5	2	2.5	3
$a_\rho \text{ fm}^2$	4,794	6,569	8,340	10,104	11,865	13,621	15,372

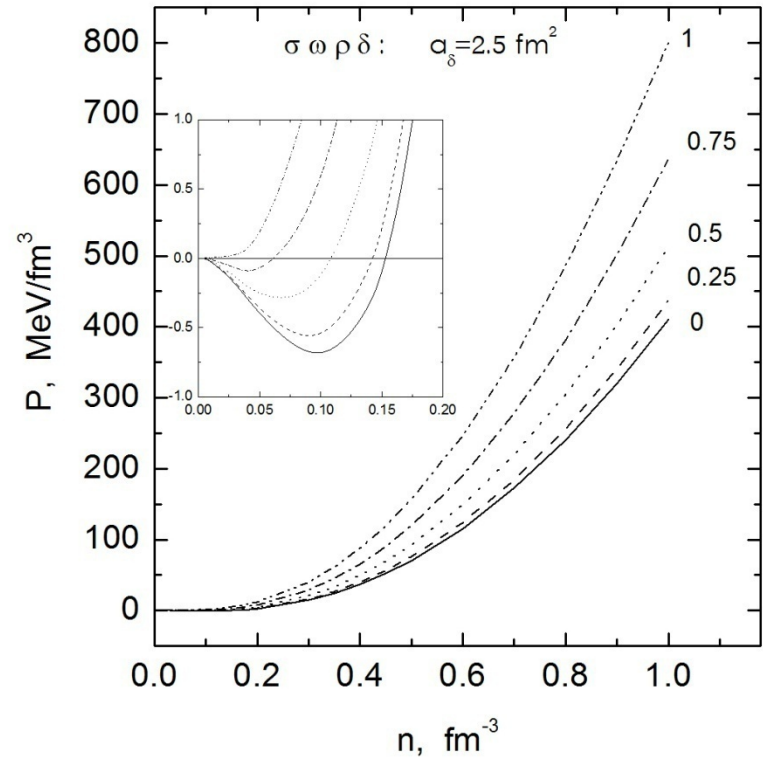
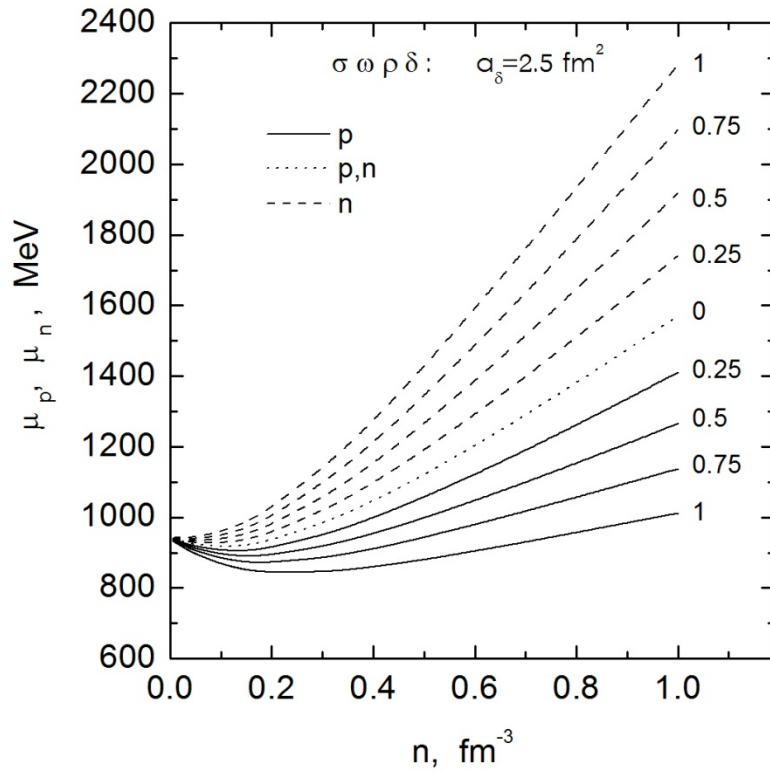
Parameters of RMF theory

Parameters	$\sigma\omega\rho$	$\sigma\omega\rho\delta$
a_σ, fm^2	9.154	9.154
a_ω, fm^2	4.828	4.828
a_δ, fm^2	0	2.5
a_ρ, fm^2	4.794	13.621
b, fm^{-1}	$1.654 \cdot 10^{-2}$	$1.654 \cdot 10^{-2}$
c	$1.319 \cdot 10^{-2}$	$1.319 \cdot 10^{-2}$

Properties of asymmetric nuclear matter



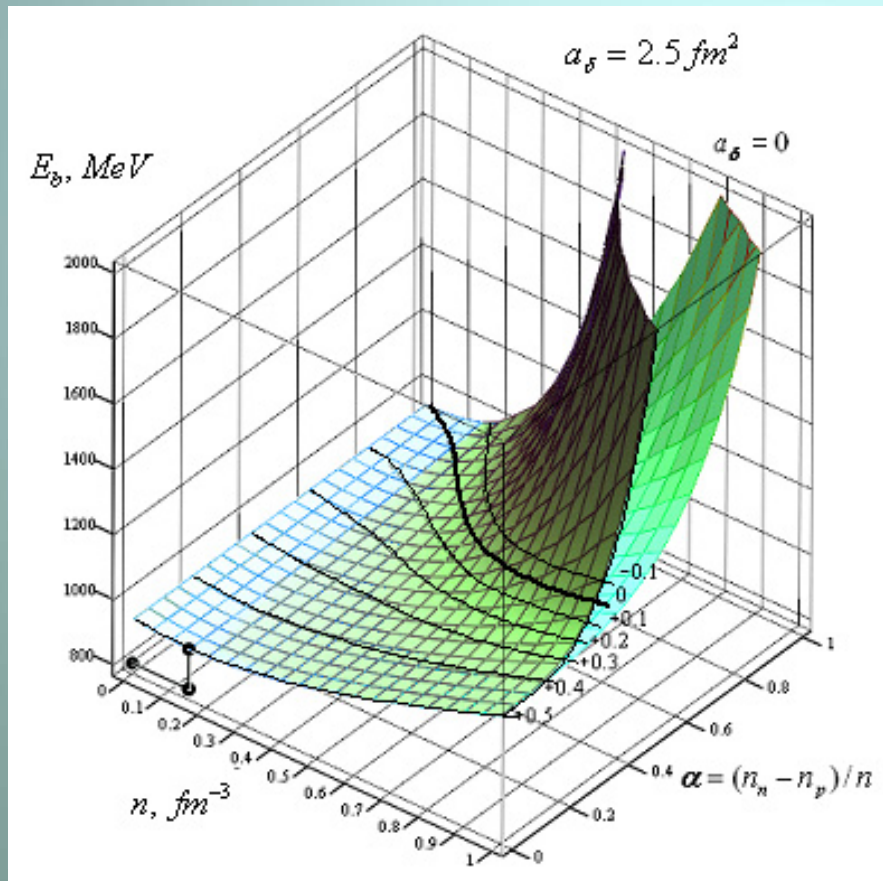
Properties of asymmetric nuclear matter



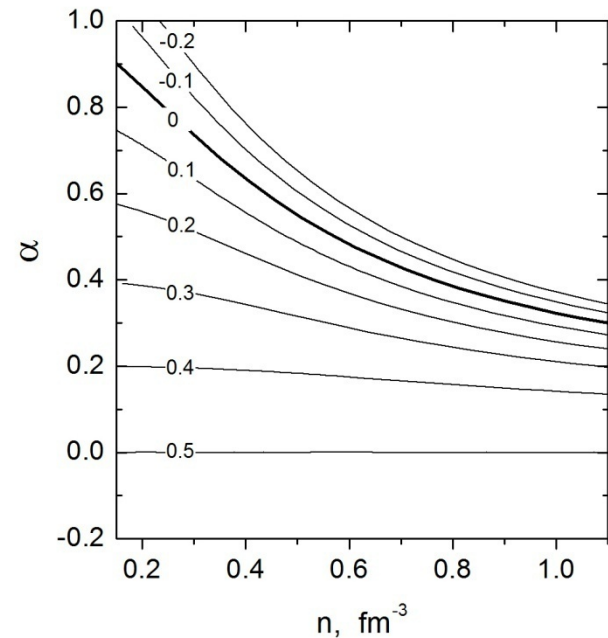
Characteristics of β -equilibrium npe- plasma

$$\varepsilon_{NM}(n, \alpha, \mu_e) = \varepsilon(n, \alpha) + \varepsilon_e(\mu_e),$$

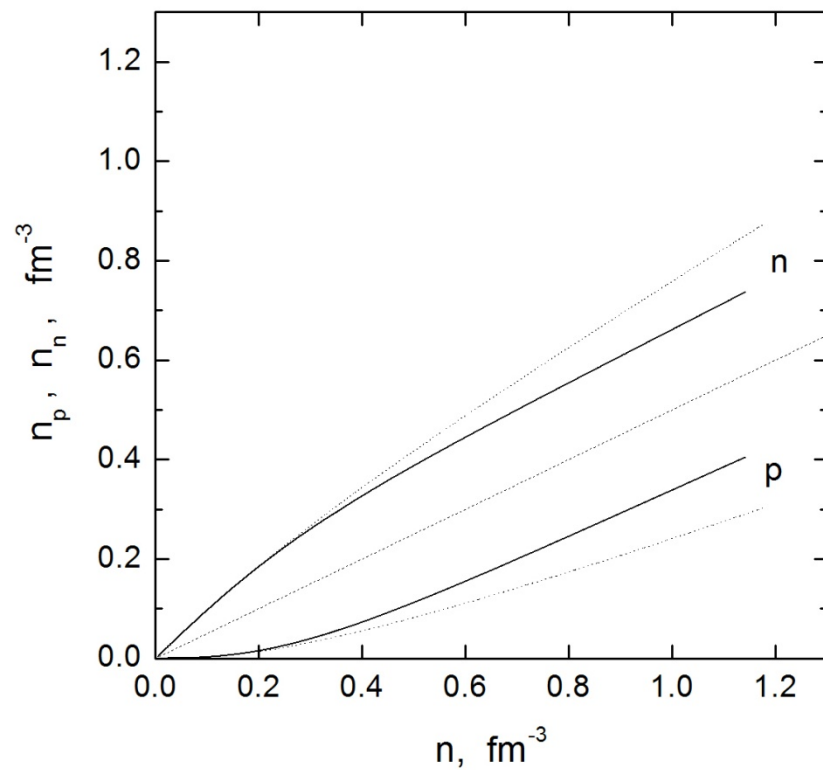
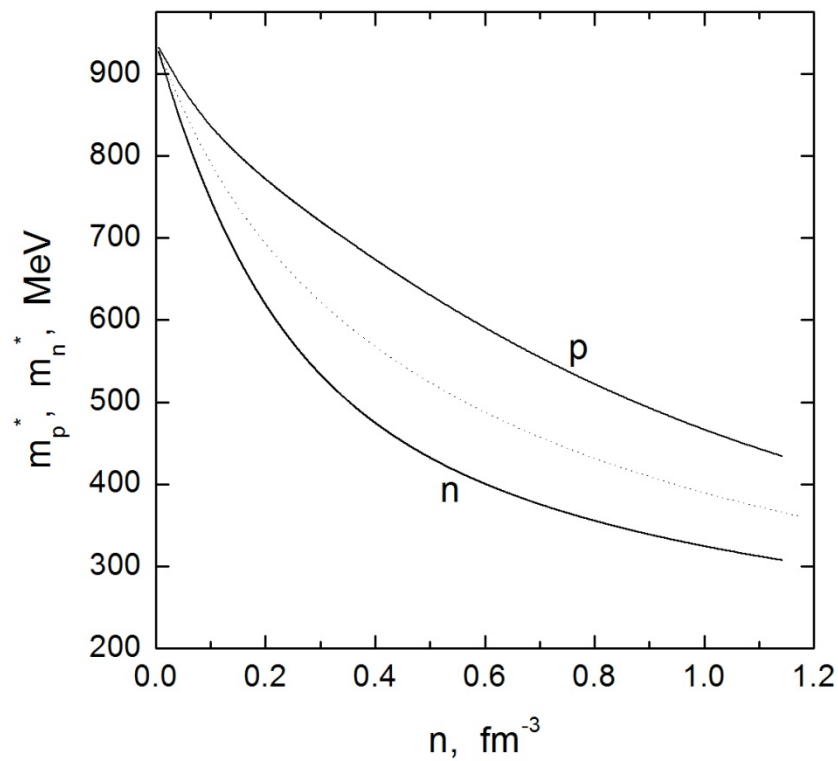
$$P_{NM}(n, \alpha, \mu_e) = P(n, \alpha) + \frac{1}{3\pi^2} \mu_e (\mu_e^2 - m_e^2)^{3/2} - \varepsilon_e(\mu_e)$$



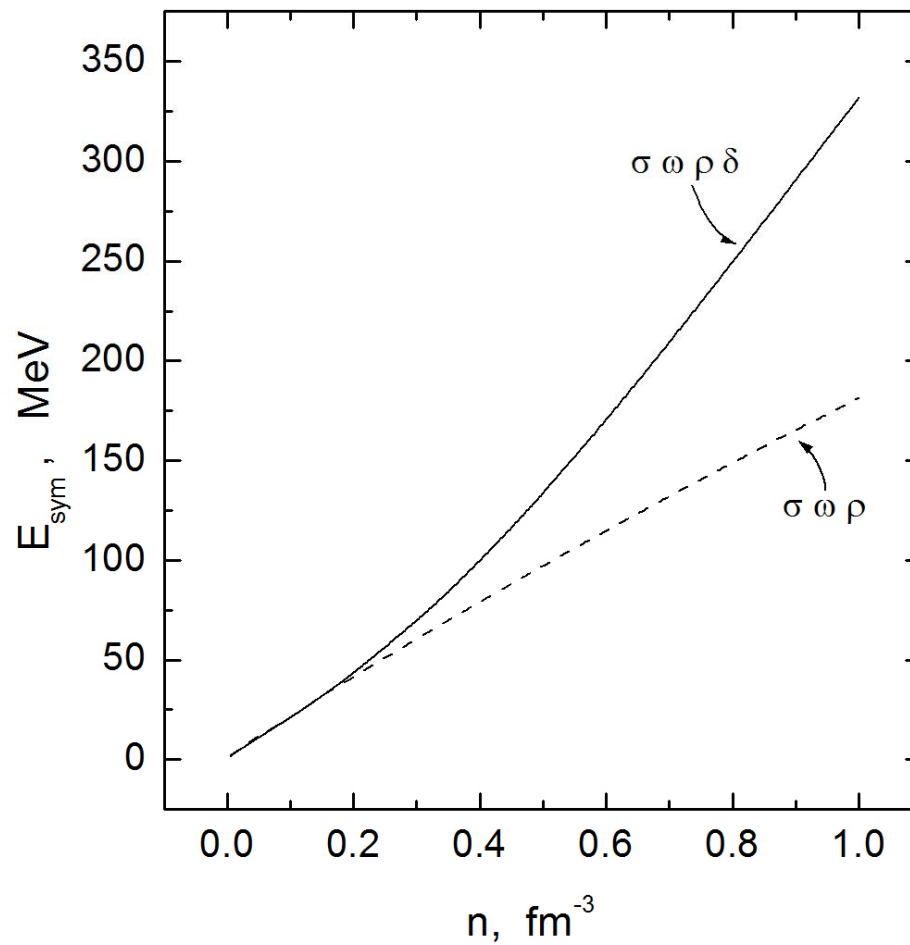
$$q = \frac{n_p - n_e}{n} = \frac{1}{2}(1 - \alpha) - \frac{n_e}{n}$$



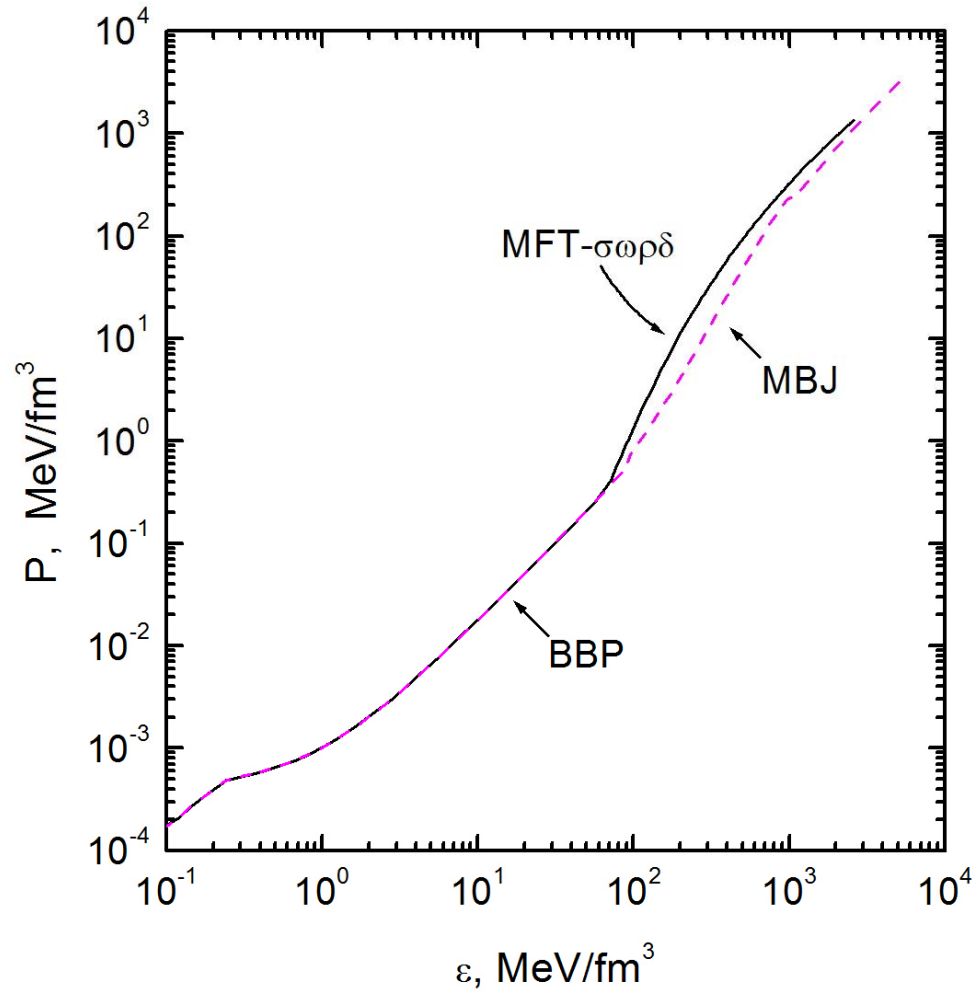
Characteristics of charge neutral and β -stable npe- plasma



Symmetry energy



EOS of neutron star matter in nucleonic phase



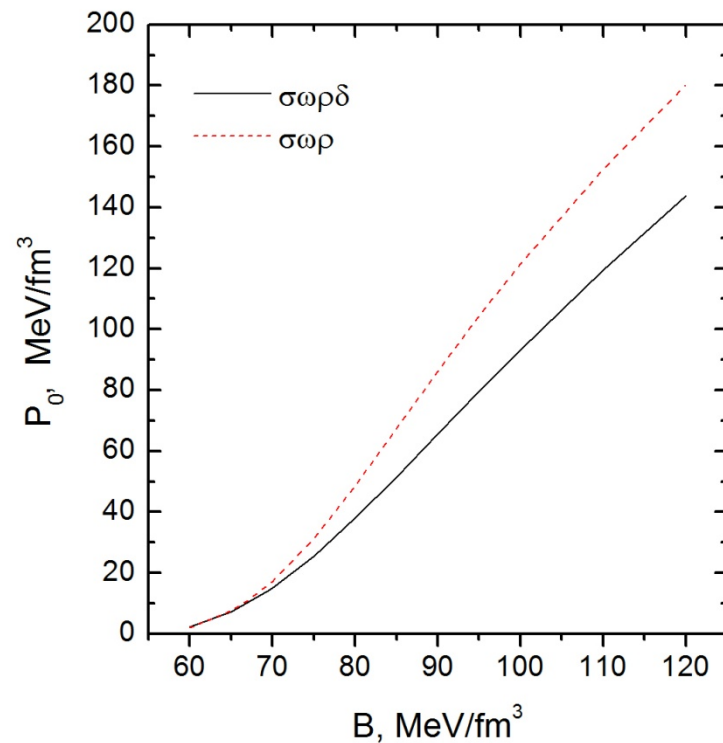
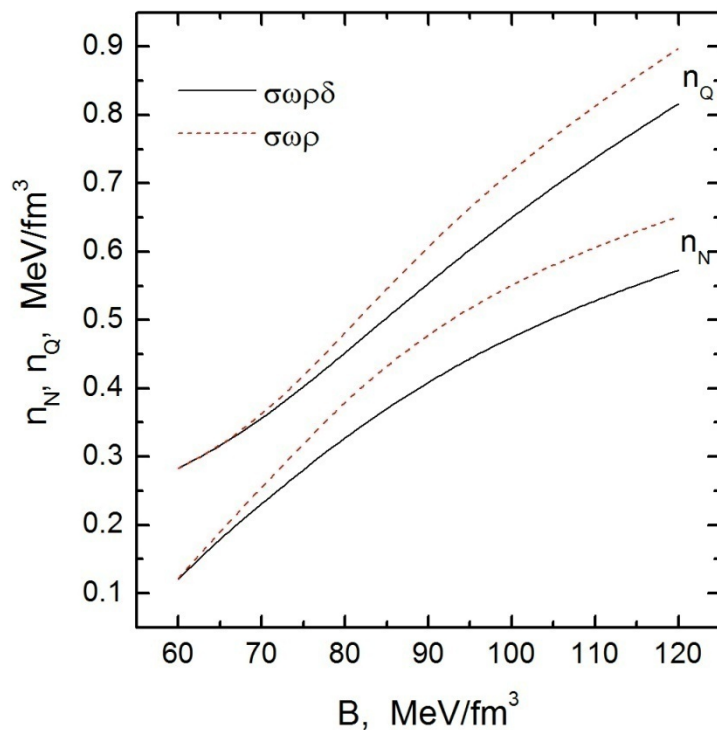
Parameters of deconfinement phase transition

MFT $\sigma\omega\rho\delta$ + MIT-bag $\alpha_s = 0.5$, $m_u = 5 \text{ MeV}$, $m_d = 7 \text{ MeV}$, $m_s = 150 \text{ MeV}$

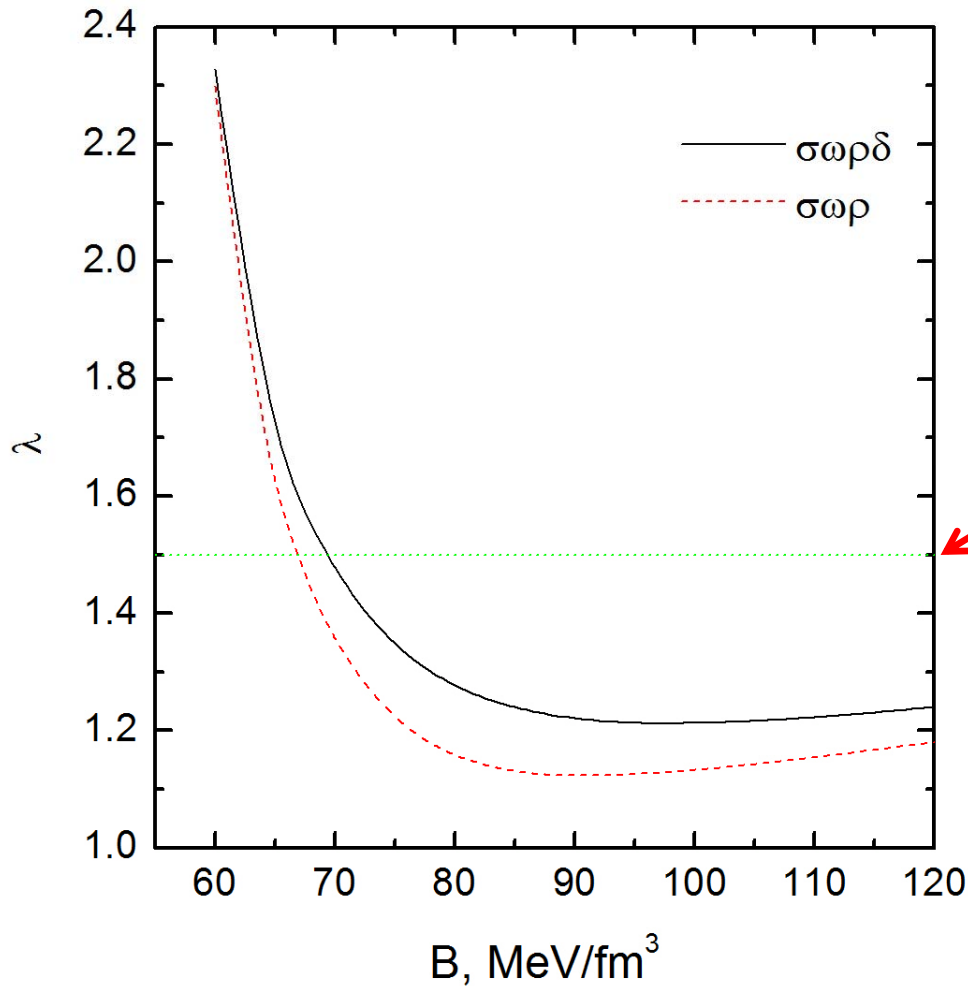
$$\mu_{NM}(P_0) = \mu_{QM}(P_0)$$

Maxwell's construction

B - bag parameter



Parameters of deconfinement phase transition



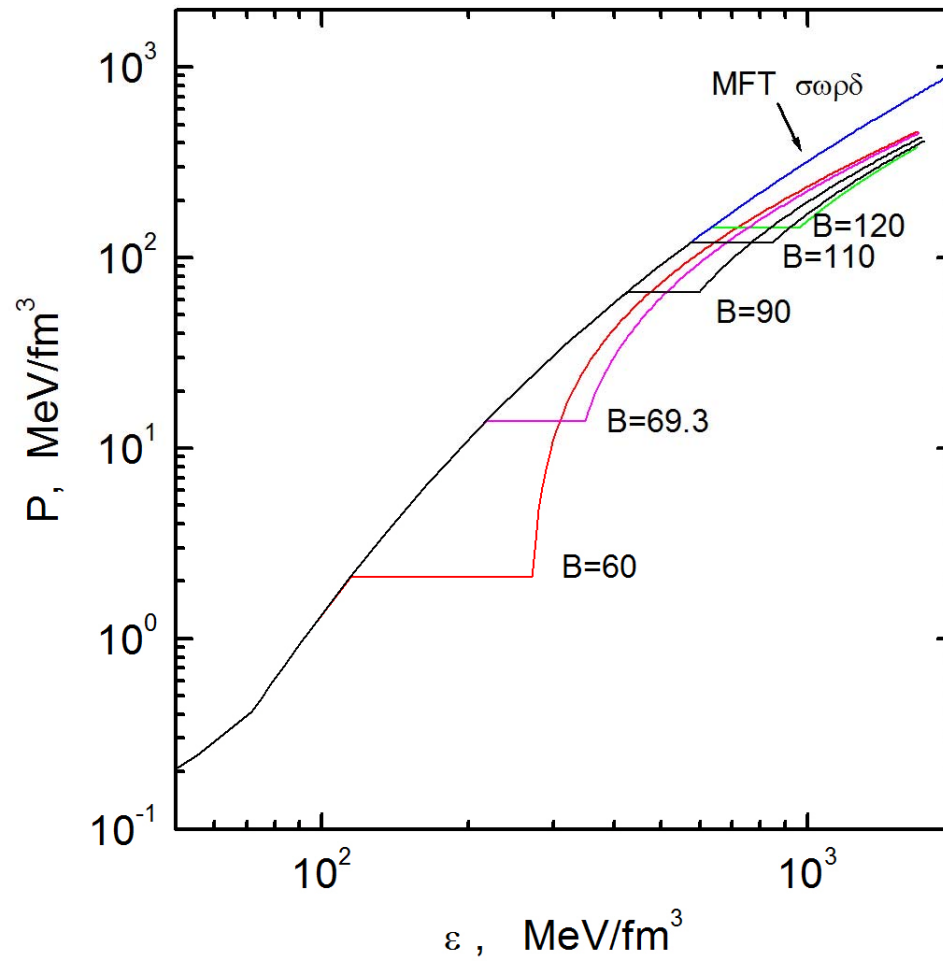
$$\lambda = \frac{\varepsilon_Q}{\varepsilon_N + P_0}$$

$$\lambda_{cr} = 3/2$$

Seidov criterium

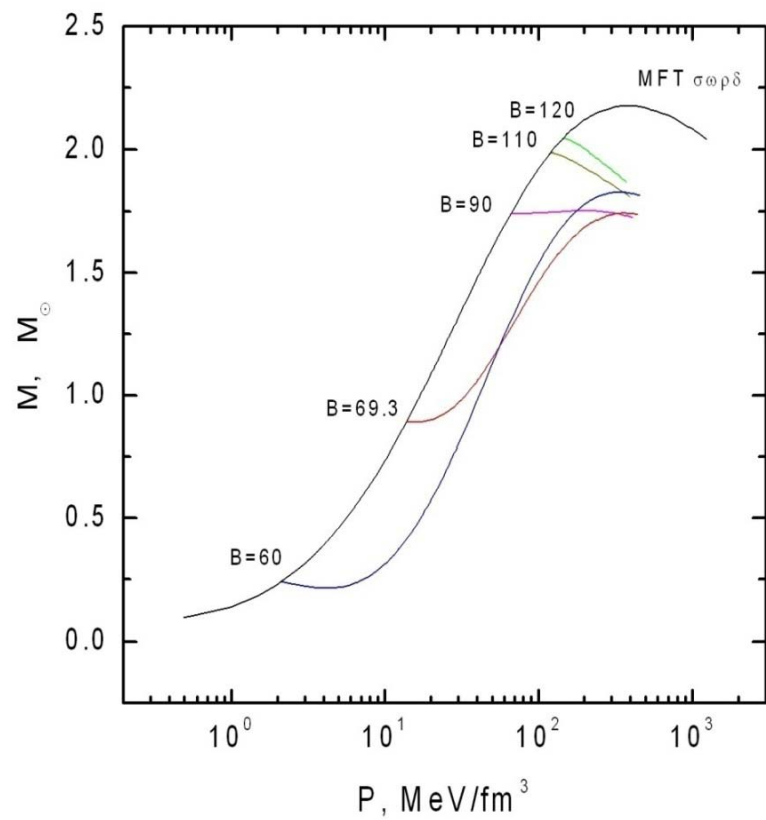
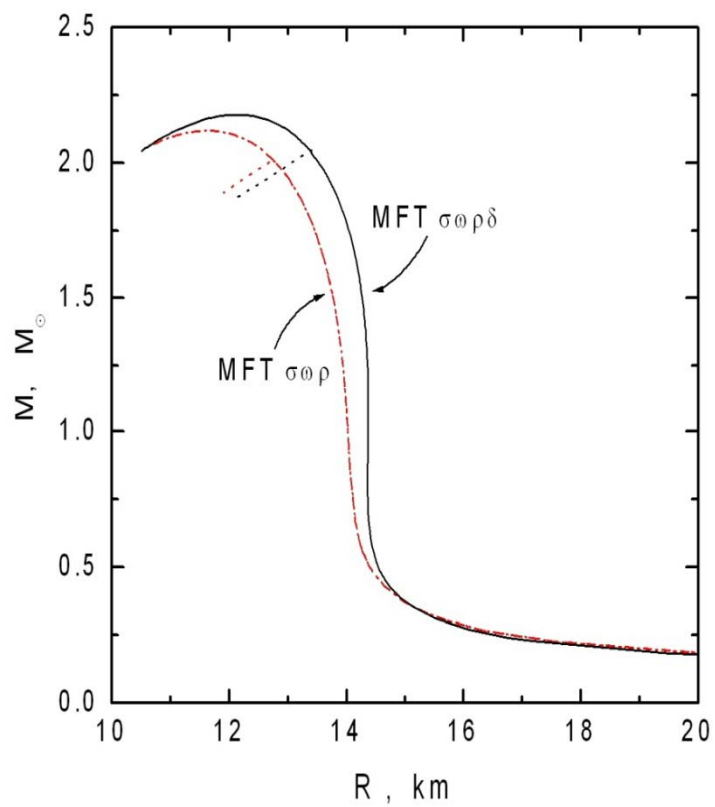
Z Seidov, *Ast.Zh.*, 48, 443, 1971

EOS with quark deconfined phase transition

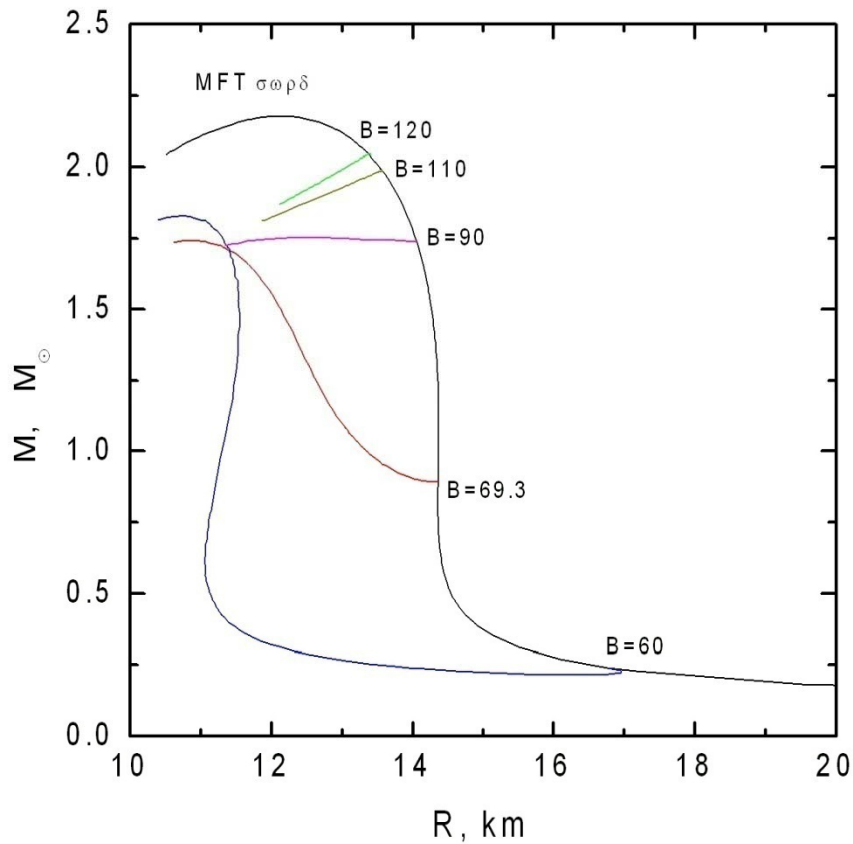


Neutron stars with quark core

TOV equations



Neutron stars with quark core



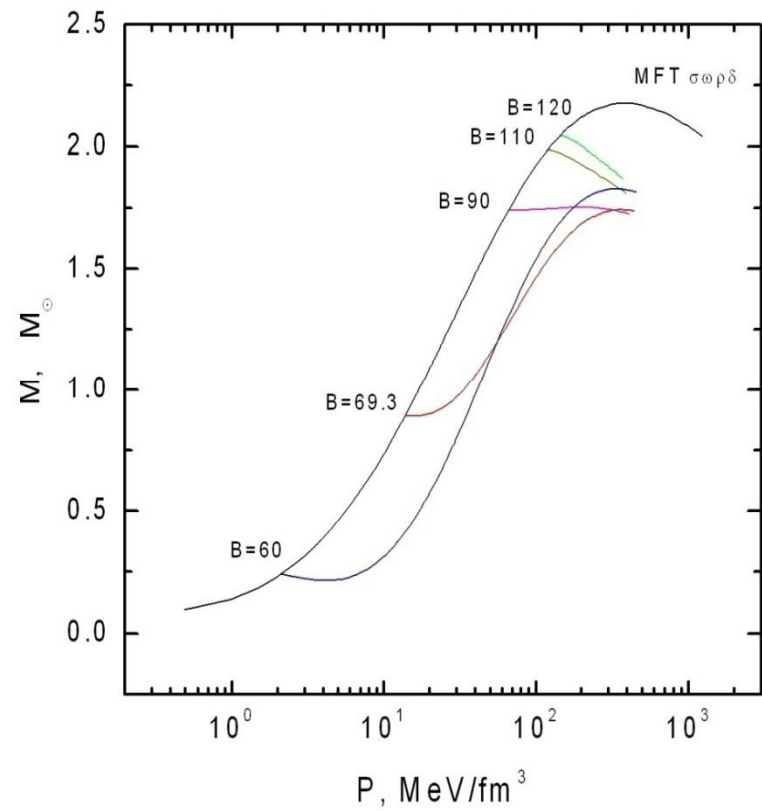
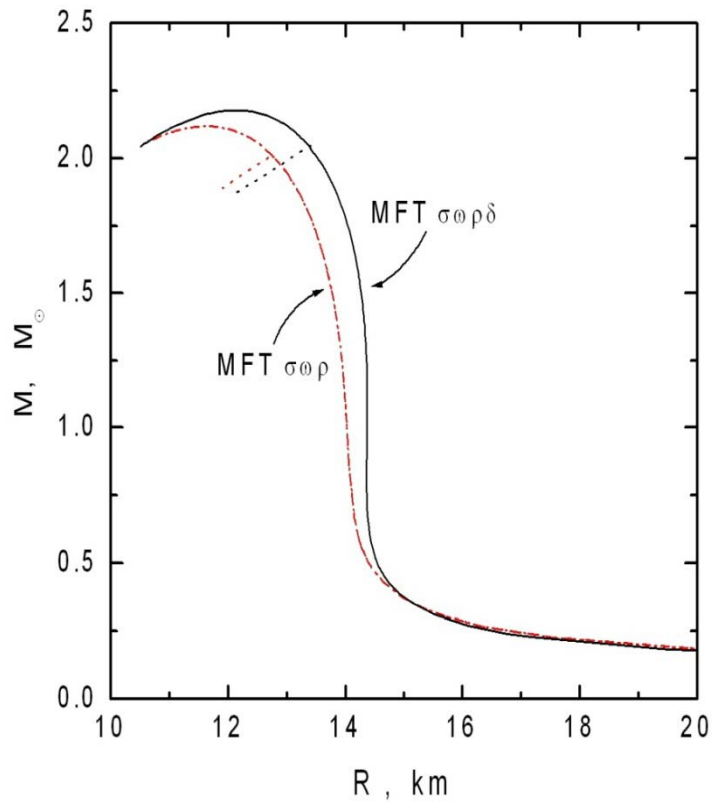
$$\lambda > 3/2 \rightarrow B < 69,3 \text{ MeV/fm}^3$$

$$\lambda_{cr} = 3/2 \rightarrow B \approx 69,3 \text{ MeV/fm}^3$$

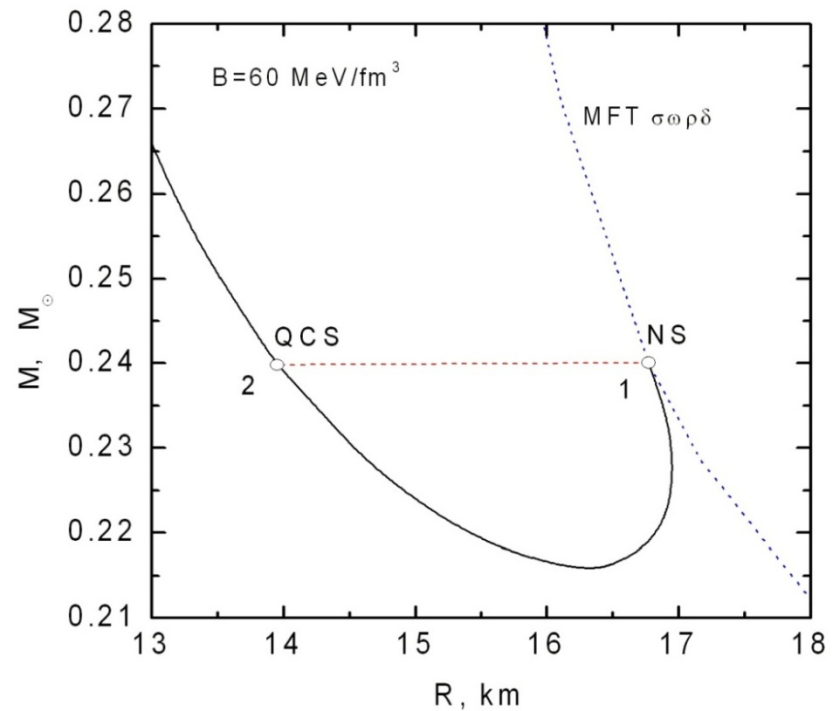
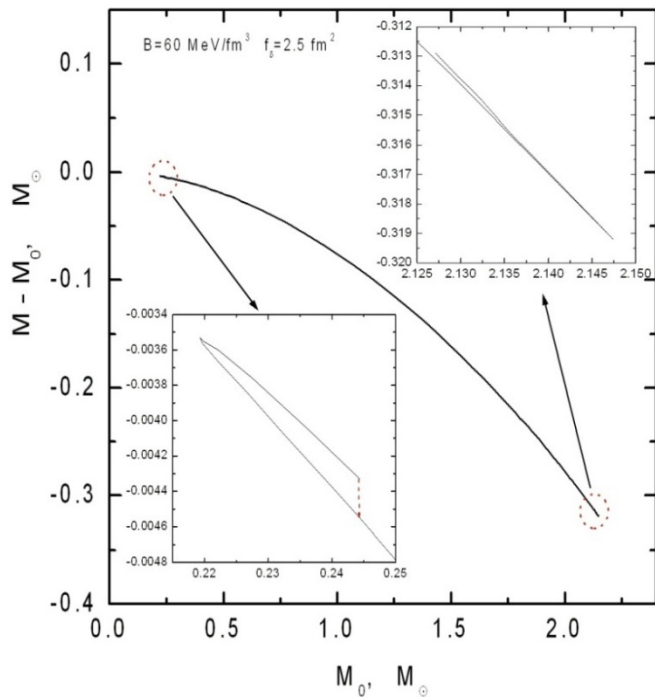
$$\lambda \leq 3/2 \rightarrow 69,3 \leq B \leq 90 \text{ MeV/fm}^3$$

$$B > 90 \text{ MeV/fm}^3 \quad \text{Unstable QP}$$

Neutron stars with quark core



Catastrophic conversion due to deconfined phase transition



$$M \approx 0.24 M_\odot$$

$$R \approx 16,77 \text{ km}$$



$$M_{core} \approx 0.087 M_\odot$$

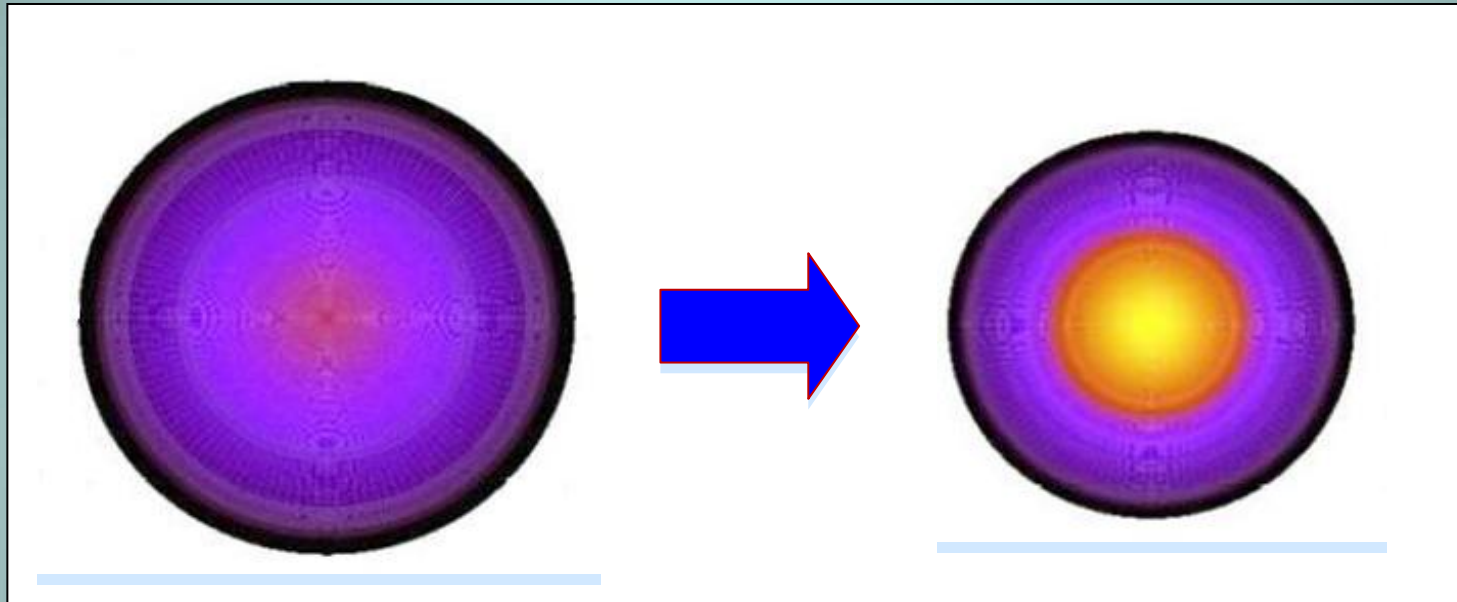
$$R_{core} \approx 4,38 \text{ km}$$

$$R \approx 13,95 \text{ km}$$

$$E_{conv} \approx 4 \cdot 10^{50} \text{ erg}$$

Catastrophic conversion due to deconfined phase transition

$$M \approx 0.24 M_{\odot}$$



$$R \approx 16.75 \text{ km}$$

$$M_{\text{core}} \approx 0.087 M_{\odot}$$

$$R_{\text{core}} \approx 4.38 \text{ km}$$

$$R \approx 13.95 \text{ km}$$

Summary

- The account of δ -meson field results in reduction of phase transition parameters, P_0, n_N, n_Q
- The density jump parameter λ , that has important significance from the point of view of infinitesimal quark core stability in neutron star, is increased.
- In case of bag parameter values $B < 69.3 \text{ MeV}/\text{fm}^3$ the condition $\lambda > 3/2$ is satisfied, and infinitesimal quark core is unstable.
- For $B > 90 \text{ MeV}/\text{fm}^3$ the quark phase is unstable.

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THANK YOU

