Dynamical Properties of the Crust of Neutron Stars: Neutrino Mean Free Path in the Presence of "Pasta Phase"



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#### Outline

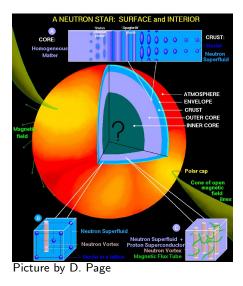
Introduction

Skyrme Hartree–Fock Calculations

Density Dependent Relativistic Mean-Field Calculations

Summary

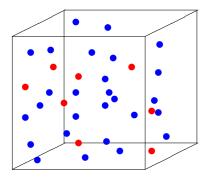
#### Introduction



- Inner core: strange baryons? quark matter?
- Outer core: homogenous superfluid neutron and proton matter, magnetic flux tube,
- Crust: nuclei, spaghetti, lasagne, superfluid neutrons,
- Athmosphere: nuclei, magnetic field.

#### Introduction

Wigner-Seitz Cell



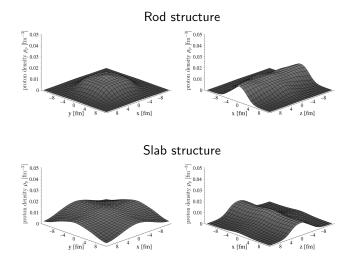
- Neutrons and protons in a Wigner–Seitz Cell as representation of nuclear matter in the crust of neutron stars.
- A cartesian cell is considered so that the whole space can be covered by repeated cells.
- In addition non-spherical structures can be observed.

- ► SLy4 was used Chabanat et al., NP A635, 231 (1998)
- HF equations were solved by using the imaginary time step method

$$\left\{-\boldsymbol{\nabla}\frac{\hbar^2}{2m_q^*(\mathbf{r})}\boldsymbol{\nabla}+U_q(\mathbf{r})-i\,\mathbf{W}_q(\mathbf{r})\cdot(\boldsymbol{\nabla}\times\boldsymbol{\sigma})\right\}\varphi_k^q(\mathbf{r})=\varepsilon_k^q\,\varphi_k^q(\mathbf{r},\boldsymbol{s})\,,$$

- The pairing of nucleons was included by means of density dependent monopole pairing force Garrido et al. PR C60, 064312 (1999)
- ► Finite temperature effects are considered within FT-HFB Theory.

More details P. Gögelein, PhD Thesis, Tübingen (2007) P. Gögelein and H. Müther, PR C76, 024312 (2007)



#### Nonrelativistic Interaction Neutrino with Quasi-Nuclei

Direct URCA processes (semileptonic reactions)

$$\nu_1 + n_2 \rightarrow e_3^- + p_4, \qquad \nu_1 + n_2 \rightarrow \nu_3 + n_4$$

The general matrix element has the form

$$M=rac{G_F \, C}{\sqrt{2}} J_\mu j^\mu,$$

where

$$J_{\mu}=iar{u}_4(V\gamma_{\mu}+A\gamma_{\mu}\gamma_5)u_2, \qquad j^{\mu}=-iar{u}_3\gamma^{\mu}(1-\gamma_5)u_1$$

Walecka "Th. Nuclear & Subnuclear Physics", (1995)

By using the Fermi's Golden Rule

$$\sigma = \sum_{f} p_{3} E_{3} \frac{1}{2} \int_{1}^{-1} d(\cos \theta) \overline{|M|}^{2},$$
  
$$\overline{|M|}^{2} = \frac{G_{F}^{2} C^{2}}{\pi} \left[ V^{2} (1 + \cos \theta) |M_{1}|^{2} + A^{2} (1 - \frac{1}{3} \cos \theta) |M_{2}|^{2} \right],$$
  
$$M_{1} = \langle \varphi_{4} | e^{i\vec{q}\vec{r}} | \varphi_{2} \rangle, \quad M_{2} = \langle \varphi_{4} | \vec{\sigma} e^{i\vec{q}\vec{r}} | \varphi_{2} \rangle,$$

where we neglected the lower components in Dirac spinors  $u \simeq \begin{pmatrix} \varphi \\ 0 \end{pmatrix}$ 

Important Remarks

The existence of electron sea (blocking factor)

$$\mu_{\rm p}+\mu_{\rm e}=\mu_{\rm n}$$

► *V<sub>cell</sub>* is the "unit" volume

$$rac{1}{\lambda} = rac{\sigma}{V_{cell}}$$

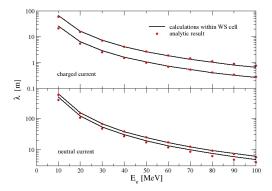
Absence of spherical symmetry

$$\vec{q}\vec{r}=q_xx+q_yy+q_zz.$$

We approximate

$$\sigma = \frac{1}{3}(\sigma_x + \sigma_y + \sigma_z)$$

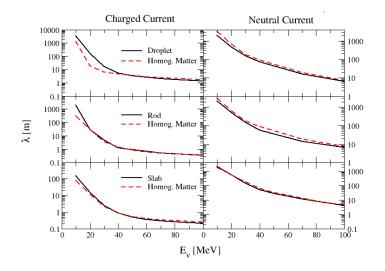
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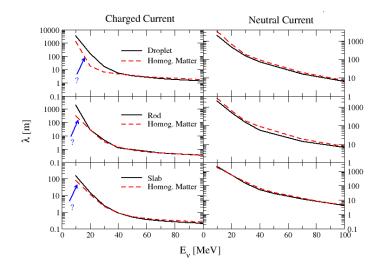
$$\frac{\sigma(E_1)}{V} = \frac{1}{\lambda} = \frac{G_F C^2}{4\pi^2} (V^2 + 3A^2) \int_{-\infty}^{E_1} dq_0 \frac{E_3}{E_1} (1 - f_3(E_3)) \int_{|q_0|}^{2E_1 - q_0} dqq S(q, q_0),$$

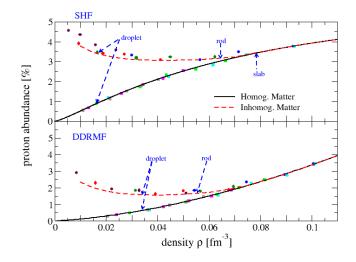
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#### Skyrme Hartree–Fock Calculations (T=1 MeV)



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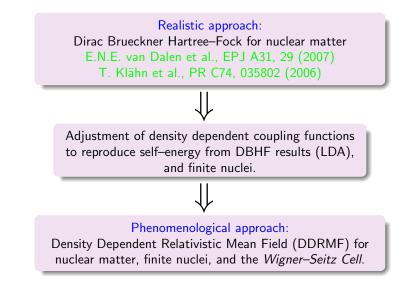




Lagrangian dens. consists of three parts: baryon, meson and interaction:

$$\mathcal{L} = \mathcal{L}_{B} + \mathcal{L}_{M} + \mathcal{L}_{int},$$

$$\begin{split} \mathcal{L}_{B} = & \bar{\Psi}(i\gamma_{\mu}\partial^{\mu} - M)\Psi, \\ \mathcal{L}_{M} = & \frac{1}{2}\sum_{i=\sigma,\delta} \left(\partial_{\mu}\Phi_{i}\partial^{\mu}\Phi_{i} - m_{i}^{2}\Phi_{i}^{2}\right) \\ & - & \frac{1}{2}\sum_{\kappa=\omega,\rho,\gamma} \left(\frac{1}{2}F_{\mu\nu(\kappa)}F_{(\kappa)}^{\mu\nu} - m_{\kappa}^{2}A_{\mu}^{(\kappa)}A^{(\kappa)\mu}\right), \\ \mathcal{L}_{int} = & - & g_{\sigma}\bar{\Psi}\Phi_{\sigma}\Psi - g_{\delta}\bar{\Psi}\tau\Phi_{\delta}\Psi \\ & - & g_{\omega}\bar{\Psi}\gamma_{\mu}A^{(\omega)\mu}\Psi - & g_{\rho}\bar{\Psi}\gamma_{\mu}\tau\mathbf{A}^{(\rho)\mu}\Psi \\ & - & e\bar{\Psi}\gamma_{\mu}\frac{1}{2}(1+\tau_{3})A^{(\gamma)\mu}\Psi, \end{split}$$
 with the field strength tensor: 
$$F_{\mu\nu(\kappa)} = & \partial_{\mu}A_{\nu(\kappa)} - \partial_{\nu}A_{\mu(\kappa)}. \end{split}$$



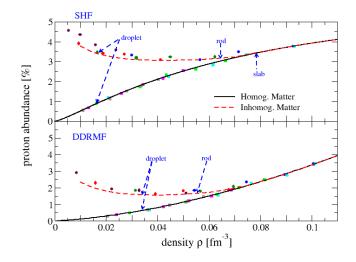
#### Relativistic Interaction Neutrino with Quasi-Nuclei

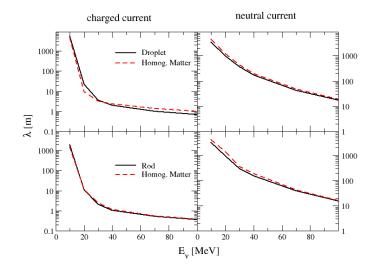
$${\cal M}=rac{G_F\,C}{\sqrt{2}}J_\mu j^\mu,$$

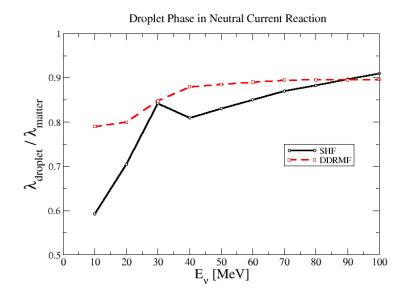
$$J_{\mu}^{CC} = i \bar{u}_{4} [F_{1}^{\nu}(q^{2})\gamma_{\mu} + F_{2}^{\nu}(q^{2})\sigma_{\mu\nu}q_{\nu} + F_{A}(q^{2})\gamma_{5}\gamma_{\mu} - iF_{\rho}(q^{2})\gamma_{5}q_{\mu}]u_{2},$$

$$\begin{aligned} J^{NC}_{\mu} &= \frac{l}{2} \bar{u}_4 [F_A(q^2) \gamma_5 \gamma_{\mu} - iF_p(q^2) \gamma_5 q_{\mu} \\ &+ (1 - 2\sin^2 \theta_W) (F_1^v(q^2) \gamma_{\mu} + F_2^v(q^2) \sigma_{\mu\nu} q_{\nu}) \\ &- 2sin^2 \theta_W (F_1^s(q^2) \gamma_{\mu} + F_2^s(q^2) \sigma_{\mu\nu} q_{\nu})] u_2, \end{aligned}$$

$$j^\mu = -iar{u}_1\gamma^\mu(1-\gamma_5)u_3$$







At which Temperature does the "Pasta Phase" disappear?

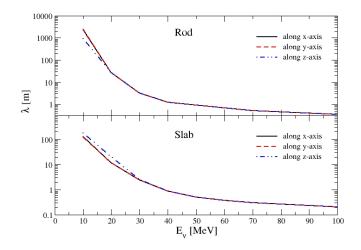
	$T_c$ (MeV)	
	SHF	DDRMF
droplet	$\gtrsim 15$	10
rod	10	5
slab	5	_

►  $T_c \gtrsim 15$  MeV from Shen et al., NP A637, 435 (1998) Relativistic TF calculations with nonlinear  $\sigma$ - and  $\omega$ - terms.

# Summary

- The relativistic and nonrelativistic interaction of neutrino with "Pasta Phase" was investigated both for charged and neutral current reactions.
- It was shown that NMFP is sensitive to the shell effects, which lead to the enhancement of proton abundance.
- The critical temperature at which the Pasta Phase disappears was found.
- ▶ The calculations of the response functions are in progress.

# Angular Dependence of NMFP



#### Iterative Procedure

- The Helmholtz equations for the mesons are solved by the conjugate gradient method.
- The Dirac equation with the scalar, vector and tensor Hartree self energy is solved by variation applying the *imaginary time step* Gögelein et al., PR C77, 025802 (2008)

